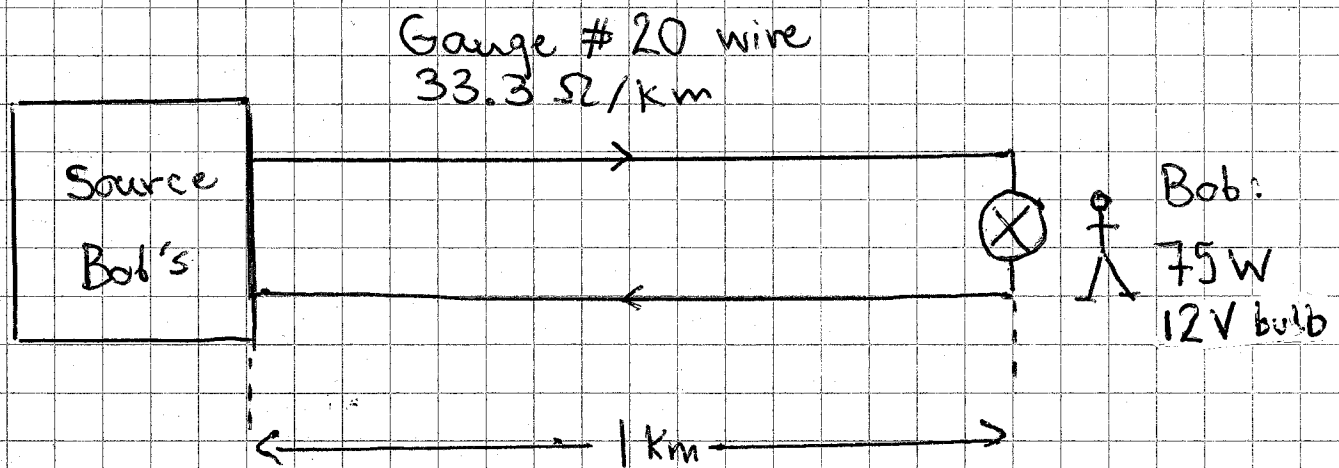


1



$$P = I \cdot V, \quad V = 12V \Rightarrow I_B = \frac{75W}{12V} = 6.25A$$

The resistance of the Bob's bulb:

$$R = \frac{V}{I} \Rightarrow R_B = 12V / 6.25A = 1.92 \Omega$$

$$\text{Another way: } P = I^2 R \Rightarrow R = \frac{P}{I^2} = \frac{75W}{(6.25A)^2} = 1.92 \Omega$$

So, the total resistance of Bob's installation

$$\text{is: } R_{\text{wire}} + R_B + R_{\text{wire}} = 2 \times 33.3 \Omega + 1.92 \Omega$$

$$= 68.52 \Omega$$

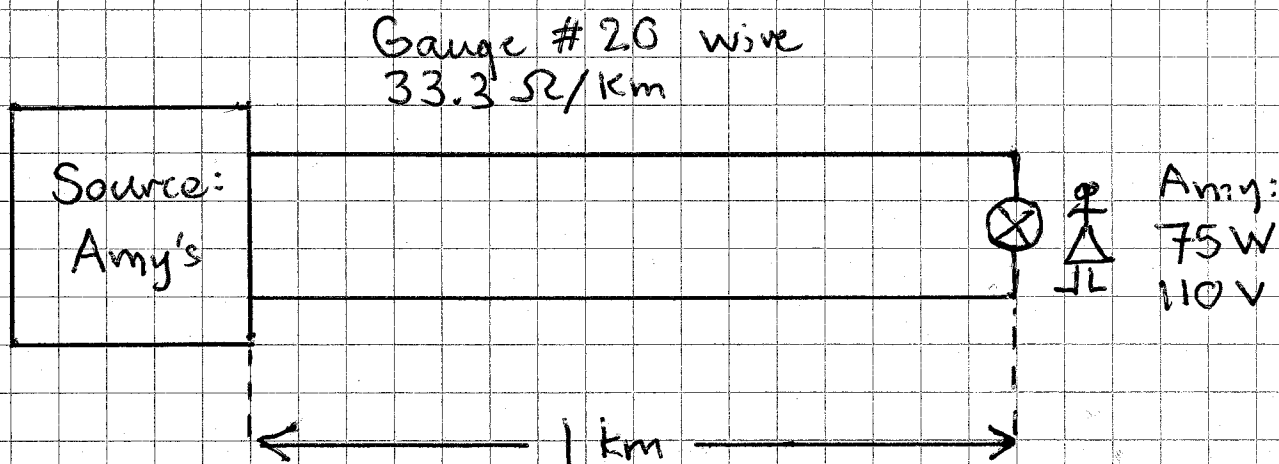
$$R_{B \text{ TOT}} = 68.52 \Omega$$

Power needed to be sent from the source is:

$$P = I^2 R \Rightarrow P_{B \text{ TOT}} = (6.25A)^2 \times 68.52 \Omega = \underline{\underline{2676W}}$$

(2601 W is dissipated in the wires).

2



$$P = I \cdot V, \quad V = 110 \text{ V} \Rightarrow I_A = \frac{75 \text{ W}}{110 \text{ V}} = 0.6818 \text{ A}$$

The resistance of the Amy's bulb is then:

$$R = \frac{V}{I} \Rightarrow R_A = \frac{110 \text{ V}}{0.682 \text{ A}} = 161.3 \Omega$$

$$\text{Another way: } P = I^2 R \Rightarrow R_A = \frac{75 \text{ W}}{(0.682 \text{ A})^2} = 161.3 \Omega$$

So, the total resistance of Amy's installation

$$\text{is: } R_{\text{wire}} + R_A + R_{\text{wire}} = 2 \times 33.3 \Omega + 161.3 \Omega = 227.9 \Omega$$

$$R_{\text{TOT}} = 227.9 \Omega$$

Power needed to be sent from the source is

$$P = I^2 R \Rightarrow P_{\text{AMY-TOTAL}} = (0.6818 \text{ A})^2 \times 227.9 \Omega = 105.94 \text{ W}$$

(only 30.94 W is dissipated in the wires).

3

An extra analysis:

The voltage of the Bob's source must be:

$$V = I \cdot R \Rightarrow V_{\text{BOB'S SOURCE}} = 68.52 \Omega \cdot 6.25 \text{ A} = 428 \text{ V}$$

While the voltage of the Amy's source must be:

$$V_{\text{AMY'S SOURCE}} = 227.9 \Omega \cdot 0.6818 \text{ A} = 155.4 \text{ V}$$

Conclusions: Bob has to use a ~~voltage~~ source of much higher voltage than Amy's source, and delivering much more power (2676 W vs. 106 W, 25 times more!)

Ergo - the transmission line is the key!

Try to use all possible means to minimize the current in the transmission line !!!

$$P_{\text{lost}} = R \cdot I^2$$

Making  $I$  smaller is much more efficient than making  $R$  small, because  $I$  is squared, and  $R$  is not.