The following equations and constants may be helpful to you. You may fill the doublesided page with handwritten notes.

$$
\begin{aligned}
& E(\vec{k})=\sum_{R} e^{i \vec{k} \cdot \vec{R}}\langle\overrightarrow{0}| \hat{H}|\vec{R}\rangle \quad E(\vec{k})=\frac{\hbar^{2} k^{2}}{2 m^{*}} \quad v(\vec{k})=\frac{1}{\hbar} \nabla_{k} E(\vec{k}) \\
& D_{\uparrow}(E)=\frac{V}{2 \pi^{2}}\left(\frac{2 m}{\hbar^{2}}\right)^{3 / 2} E^{1 / 2} \quad d S=D(E) d E \\
& m *(\vec{k})=\frac{\hbar^{2}}{\nabla_{k}^{2} E(\vec{k})} \\
& e^{i \theta}=\cos \theta+i \sin \theta \\
& \hbar=\frac{h}{2 \pi}=1.05 \times 10^{-34} \mathrm{Js}=6.58 \times 10^{-16} \mathrm{eVs} \\
& h c=1240 \mathrm{eVnm} \\
& k_{B}=1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}=8.6 \times 10^{-5} \mathrm{eV} / \mathrm{K} \\
& m_{e}=9.1 \times 10^{-31} \mathrm{~kg}=9.1 \times 10^{-28} \mathrm{~g}=0.511 \mathrm{MeV} / \mathrm{c}^{2} \\
& e=1.6 \times 10^{-19} \mathrm{C} \\
& \mu_{B}=\frac{e \hbar}{2 m_{e}}=9.27 \times 10^{-24} \mathrm{~J} / \mathrm{T}=5.8 \times 10^{-5} \mathrm{eV} / \mathrm{T} \\
& N_{A}=6.02 \times 10^{23} \text { atom } / \mathrm{mol} \\
& \varepsilon_{0}=8.85 \times 10^{-12} \mathrm{~F} / \mathrm{m} \\
& \mu_{0}=4 \pi \times 10^{-7} \mathrm{H} / \mathrm{m} \\
& f_{F D}(E, T)=\frac{1}{e^{\left(E-E_{F}\right) / k_{B} T}+1} \quad f_{M B}(E, T)=A e^{-E / k_{B} T} \\
& f_{B E}(E, T)=\frac{1}{e^{E / k_{B} T}+1} \\
& \vec{g}_{1}=2 \pi \frac{\vec{t}_{2} \times \vec{t}_{3}}{\vec{t}_{1} \cdot\left(\vec{t}_{2} \times \vec{t}_{3}\right)} \quad \vec{g}_{2}=2 \pi \frac{\vec{t}_{3} \times \vec{t}_{1}}{\vec{t}_{1} \cdot\left(\vec{t}_{2} \times \vec{t}_{3}\right)} \\
& \vec{g}_{3}=2 \pi \frac{\vec{t}_{1} \times \vec{t}_{2}}{\vec{t}_{1} \cdot\left(\vec{t}_{2} \times \vec{t}_{3}\right)} \\
& \sigma=\frac{n e^{2} \tau}{m^{*}} \\
& R_{H}=\frac{1}{n q} \\
& \omega_{p}=\sqrt{\frac{n e^{2}}{\varepsilon_{0} m^{*}}} \\
& \Delta V=S \Delta T \\
& \vec{B}=\mu_{0}(\vec{H}+\vec{M}) \\
& \vec{D}=\varepsilon_{0}(\vec{E}+\vec{P}) \\
& \chi=\frac{M}{H} \approx \frac{\mu_{0} M}{B} \\
& C_{V}=\frac{\pi^{2}}{3} D_{\imath}\left(E_{F}\right) k_{B}^{2} T \quad \frac{K_{e l}}{\sigma T}=L=2.45 \times 10^{-8} \mathrm{~W} \Omega / K^{2} \\
& n_{c}=n-i \kappa \\
& \varepsilon=\varepsilon_{1}-i \varepsilon_{2} \\
& n^{2}=\varepsilon
\end{aligned}
$$

FINAL EXAM - JUNE 13, 2014

| $\mathrm{H}^{1}$ |  | Periodic Table of the Elements |  |  |  |  |  |  |  |  |  | (C) www.elementsdatabase.com |  |  |  |  | $\mathrm{He}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Li}^{3}$ | $\mathrm{Be}^{4}$ |  |  |  |  |  | poor metals <br> nonmetals <br> noble gases <br> rare earth metals |  |  |  |  | $B^{5}$ | $C^{6}$ | $N^{7}$ | $0^{8}$ | $F^{9}$ | $\mathrm{Ne}^{10}$ |
| $\begin{gathered} 11 \\ \mathrm{Na} \end{gathered}$ | $\mathrm{Mg}^{12}$ |  |  |  |  |  | $\mathrm{Al}^{13}$ | Si ${ }^{14}$ | $P^{15}$ | $S^{16}$ | $\mathrm{Cl}^{17}$ | $\mathrm{Ar}^{18}$ |
| $K^{19}$ | $\mathrm{Ca}^{20}$ | $\mathrm{Sc}^{21}$ | $\mathrm{Ti}^{22}$ | $\mathrm{V}^{23}$ | $\mathrm{Cr}^{24}$ | $\mathrm{Mn}^{25}$ |  |  |  |  |  | $\mathrm{Fe}^{26}$ | $\mathrm{Co}^{27}$ | $\mathrm{Ni}^{28}$ | $\mathrm{Cu}^{29}$ | $\mathrm{Zn}^{30}$ | $\mathrm{Ga}^{31}$ | $\mathrm{Ge}^{32}$ | $\begin{array}{r} 33 \\ A s \end{array}$ | $\mathrm{Se}^{34}$ | $\mathrm{Br}^{35}$ | $\mathrm{Kr}^{36}$ |
| $R^{37}$ | $\mathrm{Sr}^{38}$ | $Y^{39}$ | $\mathrm{Zr}^{40}$ | $\mathrm{Nb}^{41}$ | $\begin{array}{\|c\|} \hline 42 \\ \mathrm{Mo}^{2} \\ \hline \end{array}$ | $\mathrm{Tc}^{43}$ | $\mathrm{Ru}^{44}$ | $\mathrm{Rh}^{45}$ | $\mathrm{Pd}^{46}$ | $\mathrm{Ag}^{47}$ | $\mathrm{Cd}^{48}$ | $1 n^{49}$ | $\begin{gathered} 50 \\ \mathrm{Sn} \end{gathered}$ | $S b^{51}$ | $T e^{52}$ | $\left.\right\|^{53}$ | $\times{ }^{54}$ |
| $\mathrm{Cs}^{55}$ | $\begin{gathered} 56 \\ \mathrm{Ba} \end{gathered}$ | ${ }^{57}$ | $\mathrm{Hf}^{72}$ | $\mathrm{Ta}^{73}$ | $W^{74}$ | $\mathrm{Re}^{75}$ | $\begin{array}{\|c\|} \hline 76 \\ \mathrm{Os} \end{array}$ | $\mathrm{Ir}^{77}$ | $\begin{array}{\|c\|} \hline 78 \\ \mathrm{Pt}^{2} \\ \hline \end{array}$ | $\begin{array}{r} 79 \\ \mathrm{Au} \end{array}$ | $\begin{gathered} 80 \\ \mathrm{Hg} \end{gathered}$ | $\mathrm{Tl}^{81}$ | $\begin{array}{\|c\|} \hline 82 \\ \mathrm{~Pb} \end{array}$ | $\mathrm{Bi}^{83}$ | $\begin{gathered} 84 \\ \mathrm{PO}^{84} \end{gathered}$ | $\mathrm{At}^{85}$ | $\mathrm{Rn}^{86}$ |
| ${ }^{\mathrm{Fr}}$ | $\mathrm{Ra}^{88}$ | $\begin{array}{r} 89 \\ \mathrm{Ac} \end{array}$ | $\begin{array}{\|c\|} \hline 104 \\ \hline \text { Unq } \end{array}$ | $\begin{array}{r} 105 \\ \text { Unp } \end{array}$ | $\begin{array}{\|c\|} \hline 106 \\ \hline \text { Unh } \end{array}$ | $\begin{array}{\|c\|} \hline 107 \\ \hline \text { Uns } \end{array}$ | $\begin{array}{\|r\|} \hline 108 \\ \text { Uno } \end{array}$ | $\begin{array}{\|c\|} \hline 109 \\ \hline \text { Une } \end{array}$ | Unn ${ }^{110}$ |  |  |  |  |  |  |  |  |


| $\mathrm{Ce}^{58}$ | Pr | Nd | Pm | $\mathrm{Sm}^{62}$ | $\mathrm{Eu}^{63}$ | $\mathrm{Gd}^{64}$ | $\mathrm{~Tb}^{65}$ | $\mathrm{Dy}^{66}$ | $\mathrm{Ho}^{67}$ | $\mathrm{Er}^{68}$ | $\mathrm{Tm}^{69}$ | $\mathrm{Yb}^{70}$ | $\mathrm{Lu}^{71}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Th}^{90}$ | Pa | $\mathrm{U}^{92}$ | $\mathrm{~Np}^{93}$ | Pu | $\mathrm{Am}^{95}$ | $\mathrm{Cm}^{96}$ | $\mathrm{Bk}^{97}$ | $\mathrm{Cf}^{98}$ | $\mathrm{Es}^{99}$ | Fm | Md | No | $\mathrm{Lr}^{103}$ |

