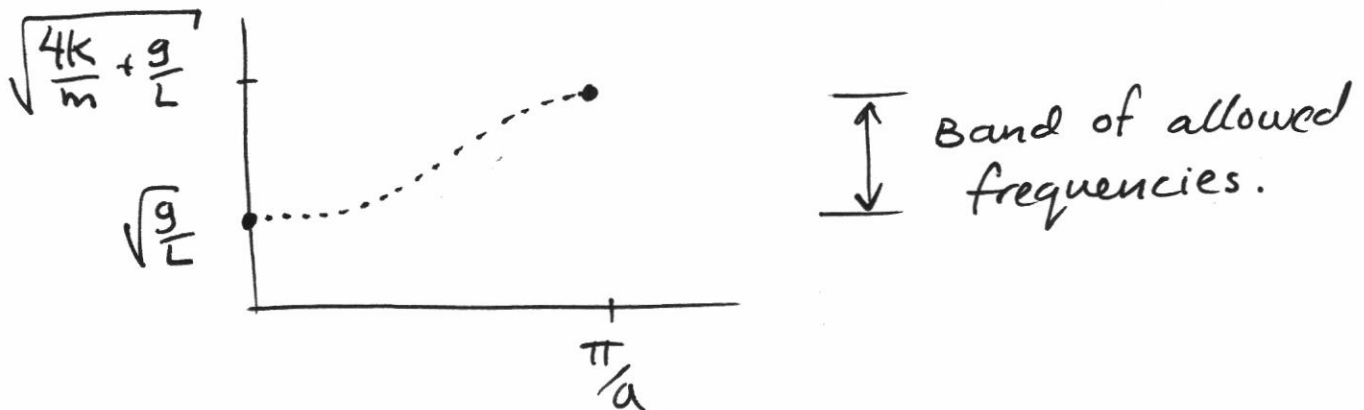


Discuss the forbidden freqs of the coupled pendulum system.

From HW #2

$$\omega = \sqrt{\frac{4K}{m} \sin^2 \frac{ka}{2} + \frac{g}{L}}$$

check limits  $k=0$ ,  $k=\frac{\pi}{a}$



Using the billiard ball demo:

move the 8 ball very slowly ( $\omega < \sqrt{\frac{g}{L}}$ )

move the 8 ball very fast ( $\omega > \sqrt{\frac{4K}{m} + \frac{g}{L}}$ )

(2)

Last time  $\langle n_k \rangle = \frac{1}{e^{\hbar\omega_k/k_B T} - 1}$

Examples of exam questions:

- How many phonons occupy the highest freq mode of a diamond? (Approximation question)
- At what temperature does the highest freq mode of a diamond have  $\langle n_k \rangle < 1/2$  (Approx question)
- Show that  $\langle n_k \rangle$  increases linearly with  $T$  for  $k_B T \gg \hbar\omega_k$ .
- How fast does a phonon move through a material if  $\omega_k \ll \omega_{\text{Debye}}$ ? (Approximation question)

(3)

## FINAL REMARKS ABOUT PHONONS

### \* Relationship to Noether's Thm:

Once a phonon<sub><sup>wave packet</sup></sub> is launched in a "perfect crystal" it travels all the way across the crystal.

The quantity  $\hbar k$  is called the phonon momentum.

The phonon momentum is conserved.

\* In real systems, phonons are always being created and destroyed, keeping the system in thermal eqb such that

$$\langle n_k \rangle = \frac{1}{e^{\hbar \omega_k / k_B T} - 1} \quad \text{for all modes.}$$

(4)

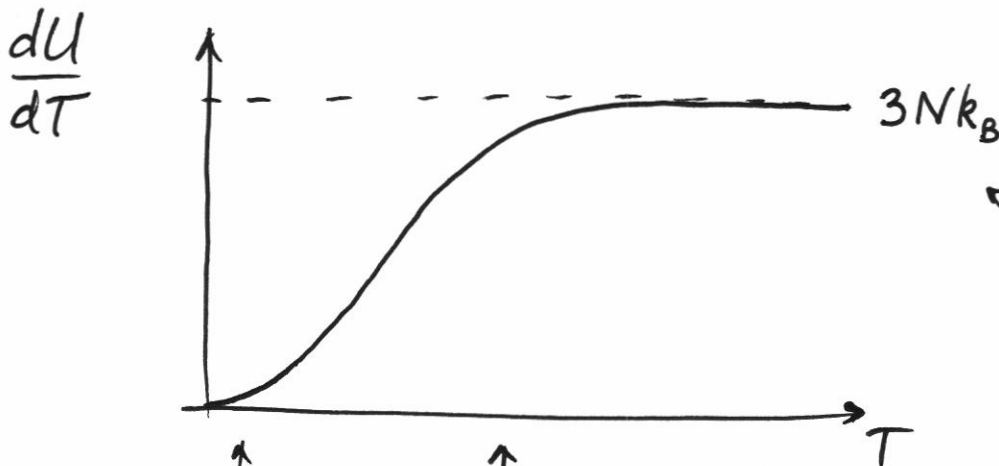
# \* SUMMARY OF LATTICE HEAT CAPACITY

Correct model for lattice vibrational energy

$$U(T) = \sum_{\text{all } k} \hbar \omega_k (n_k + 1/2)$$

↑  
depends on T

Heat capacity (if we neglect small changes in  $\omega_k$  as a function of temperature)



Classical prediction of equipartition thm.

Every mode stores energy  $k_B T$ .