FINAL EXAM - April 24, 2006 7:30 pm - 9:20 pm

This exam is closed book and closed notes except for the information on this cover sheet. You may use a calculator and a ruler. Please do all your work in the blue books. Only the blue books will be graded! Show all your work.

Budget your time wisely! Not all questions are of equal difficulty.

Equations that may be useful:

$$\begin{split} \vec{\mathbf{a}}_{\text{rel}} &= \vec{\mathbf{a}} - 2\vec{\boldsymbol{\omega}} \times \vec{\mathbf{v}}_{\text{rel}} - \vec{\boldsymbol{\omega}} \times (\vec{\boldsymbol{\omega}} \times \vec{\mathbf{r}}) \\ \vec{\boldsymbol{\omega}} &= \Omega \hat{\boldsymbol{z}} \qquad \hat{\boldsymbol{z}} = \cos\theta \, \hat{\mathbf{r}} - \sin\theta \, \hat{\boldsymbol{\theta}} \qquad \lambda = \frac{\pi}{2} - \theta \\ x' &= \gamma (x - vt) = x \cosh\beta - ct \sinh\beta \qquad x = \gamma (x' + vt') = x' \cosh\beta + ct' \sinh\beta \\ ct' &= \gamma \left(ct - \frac{v}{c} x \right) = ct \cosh\beta - x \sinh\beta \qquad ct = \gamma \left(ct' + \frac{v}{c} x' \right) = ct' \cosh\beta + x' \sinh\beta \\ x^2 - c^2 t^2 &= x'^2 - c^2 t'^2 \\ \frac{v}{c} &= \tanh\beta \qquad \gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \cosh\beta \qquad \frac{v}{c} \gamma = \sinh\beta \\ \tanh(\alpha + \beta) &= \frac{\tanh\alpha + \tanh\beta}{1 + \tanh\beta} \qquad \frac{u}{c} = \tanh\alpha \implies \frac{w}{c} = \tanh(\alpha + \beta) = \frac{\frac{u}{c} + \frac{v}{c}}{1 + \frac{uv}{2}} \end{split}$$

$$\tanh(\alpha + \beta) = \frac{\tanh \alpha + \tanh \beta}{1 + \tanh \alpha \tanh \beta} \qquad \frac{u}{c} = \tanh \alpha \implies \frac{w}{c} = \tanh(\alpha + \beta) = \frac{\frac{u}{c} + \frac{v}{c}}{1 + \frac{uv}{c^2}}$$

$$E = \gamma mc^2 = mc^2 \cosh \beta \qquad p = \gamma mv = mc \sinh \beta$$

$$E^2 - p^2c^2 = m^2c^4 = E'^2 - p'^2c^2$$

$$E'_{x} = E_{x}$$

$$E'_{y} = \gamma \left(E_{y} - \nu B_{z} \right)$$

$$E'_{z} = \gamma \left(E_{z} + \nu B_{y} \right)$$

$$B'_{z} = B_{x}$$

$$B'_{y} = \gamma \left(B_{y} + \frac{\nu}{c^{2}} E_{z} \right)$$

$$B'_{z} = \gamma \left(B_{z} - \frac{\nu}{c^{2}} E_{y} \right)$$

$$\left|\vec{\mathbf{E}}\cdot\vec{\mathbf{B}} = \vec{\mathbf{E}}'\cdot\vec{\mathbf{B}}'\right|^{2} = \left|\vec{\mathbf{E}}'\right|^{2} - c^{2}\left|\vec{\mathbf{B}}'\right|^{2}$$