LAB 8: Magnetism and Electric Current

I. The Right-Hand Rule (a Testing experiment)

II. What's the charge? (an Observation experiment)

III. Insulators vs. conductors (a Testing experiment)

IV. Current in a DC circuit with multiple capacitors (a Testing experiment)

V. Practice with RC circuits

IV. Magnetic induction practice—a take-home worksheet, due from every student by 6:00 p.m. on Tuesday, June 6 (5 points)

II. Magnetic induction basics

I. An electric motor (an Application experiment)

LAB Policies and General Information

Lab Types, Reports and Scoring

Rubric O (Observation experiment)

Rubric T (Testing experiment)

Rubric A (Application experiment)

Experimental Uncertainty

Sources of uncertainty in measurements

Comparing uncertainties

Reducing uncertainties

Calculating with measured values: Combining uncertainties

Summary: Your strategy for dealing with uncertainty in these labs

LAB 1: Introduction—a take-home worksheet, due from every student by 6:00 p.m. on Tuesday, April 10 (10 points)

I. Lab/course policies

II. Vector math review
Lab Policies and General Information

The purpose(s) of these labs: The lab portion of this course is not to test what you (may) already know about physics. Rather, it’s to help you sharpen that knowledge more fully and clearly, in a very practical setting — where you encounter first-hand the fundamental “testing” nature of science. Lab is not directly tested on the exams (nor does it prepare you directly for exams — though you’ll be practicing verbal/writing skills useful on the exams).

Unlike in other courses, moreover, these labs are not “cookbook” recipes of procedures that you just plod through. To a large extent, you will design your own experiments — so you must come to lab prepared. Your TA is there to act as your guide only in a minimal sense — as a resource or a sounding board, not to demonstrate or explain exactly what to do. And — like the rest of this course — you must continually hone the all-important skill of putting into words what you think and discover; you must be able to explain, reconcile and summarize your reasoning.

So resolve right now to embrace the real purposes of lab and take full advantage of it: (i) to apply physics principles appropriately; and (ii) to make sense of them, so that you can, likewise, convey that sense to others.

Attendance: Lab is a team effort; you will work each week as part of a group of 3. Usually, you will be allowed to form your own groups, but note that your TA has full discretion in this matter. And he/she may allow the same groups to form each week or ask you to form new ones.

Your participation is required throughout every lab session. In order to be counted as present for the lab (i.e. contributing to your group and receiving a non-zero score for that lab), you must arrive no more than “a few minutes” late (and you must stay until your group has turned in its lab write-up). What does “a few minutes” mean? That is up to your TA — he/she will tell you this in Lab 1 (either in person or via the Lab Syllabus, or both). Whatever rule he/she sets for that late “cutoff” is what you go by. And then note: Lab credit is not given just for “warming the chair.” To earn a share of the points each week, you must participate actively and contribute genuinely to your group. Your TA has full discretion to deduct points from your lab credit for marginal (or non-) participation.

Your lab grade: Your lab is worth 10% of your overall course grade (so: 100 points out of 1000 total possible for the course). There are 9 labs in all, each worth 1 to 1.5% (10 to 15 points out of 1000) of your total grade. This may seem trivial, but NOTE: For any lab you miss (i.e. score a 0 for that lab), 5% will be deducted from your total course score (not just your lab score). This is a serious penalty — DO NOT SKIP ANY LABS. (Notice that there is a chance during Week 10 to make up labs — but no more than two — that you missed during the term.)

There is one lab write-up per group, but each group member must clearly put his/her name and student ID at the top of the write-up in order to obtain credit. You will usually need to supply your own paper for the write-up—do not plan to write on the pages of this lab packet unless it specifically gives you space and directions to do so. When using your own paper, you should use whatever format your TA may prefer/specify, if any. (See the next page for more specifics about the content of the lab write-ups.)

The lab write-up is done entirely during the 3-hour lab; there is nothing more to do afterward. But you’d better read the lab ahead of time and familiarize yourself with what’s involved. Your TA will not be taking much time to explain it to you — you know how to read. As a professional, you are ALWAYS expected to arrive having read and prepared. And each write-up requires you to explain carefully (but consisely): Besides the physics, you’ll need to justify your experiment, its results and conclusions — accounting, too, for experimental uncertainty.
Lab Types, Reports and Scoring

**Lab Types:** You will conduct 3 different types of lab experiments during this term.

**A. Observation experiments.** These are intended for students to learn skills such as changing one variable at a time, clearly recording and representing observations, and making accurate observations without mixing them with explanations. This is the first step of the experimental cycle, and allows you to observe phenomena, look for patterns in data, and start to devise explanations (once observations are carefully completed).

**B. Testing experiments.** Once explanations have been devised, the next step is to conduct an independent test students design that will test a hypothesis based on a specific explanation or rule. This helps you practice the skill of making predictions about the outcome of an experiment based on an explanation/rule/relationship. For a testing experiment, you can’t just do the experiment and record what happens – they must have a predicted outcome based on some explanation – and if the outcome of the experiment agrees with the prediction it gives confidence that the explanation may be correct, but if it disagrees, then you know the explanation is incorrect. In order to make this judgment, you also need to apply basic uncertainty calculations. (A guide for understanding uncertainty is included in this packet.)

**C. Application experiments.** The third type of experiment is the application experiment, where you apply some explanation/rule/relationship that you have tested enough that you think it is ‘good’, and you apply it to understand a new situation. Some application experiments require that you determine some unknown quantity multiple ways – in order to determine if the methods are consistent, it is necessary to apply basic uncertainty analysis. By performing this sequence of experiments, it is possible to explore and devise a physics relationship, test it, and when you are convinced it is good, apply it to understand a new situation – providing you with a complete understanding of the basic physics relationships (equations). By designing your own experiments, it gives you creative control, and assures that you understand the steps that you perform, as they are done by your conscious choice, and not by following instructions or ‘playing around.’

**Your group lab write-up** is not a formal report, but it does need to be clear. The lab will often include a reminder of the general items that must always be included within your write-up (related to the type of experiment: observation, testing, or application). It may also have specific questions for you to answer and/or tasks to complete (answer and document) in your write-up. Your information does not need to be presented in paragraph form; use short, clear and complete sentences to address the required points succinctly. You may use equations and/or diagrams instead of trying to write the math out in words.

For a sample lab write-up, click here.

**Your TA will score each write-up** by evaluating a selected subset (usually 5-10) of the items required in the lab. Each item will be scored out of a possible of 3 points, according to a rubric—a scoring guide. For each of these three types of experiments, there is rubric for you and the TA to use to evaluate your work—see the next three pages. Plan to bring these rubrics (and also the section covering experimental uncertainty) to lab with you, so that you can check your write-up as you work on it. Then your TA will take your total lab score that week and convert it to a scale out of 10 or 15 points—1% or 1.5% of your overall course grade. (Again, see the online Course Syllabus for more about grading policies.)

To see how the above sample lab write-up would be scored, click here.
<table>
<thead>
<tr>
<th>Scientific Ability</th>
<th>Missing (0 points)</th>
<th>Inadequate (1 point)</th>
<th>Still needs improvement (2 points)</th>
<th>Adequate (3 points)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Clearly identify the phenomenon to be investigated.</td>
<td>No mention is made of the phenomenon to be investigated.</td>
<td>An attempt is made to identify the phenomenon to be investigated, but it is described in a confusing manner.</td>
<td>The phenomenon to be investigated is described, but there are minor omissions or vague details.</td>
<td>The phenomenon to be investigated is clearly stated.</td>
</tr>
<tr>
<td>2. Design a reliable experiment that investigates the phenomenon.</td>
<td>The experiment does not investigate the phenomenon.</td>
<td>The experiment involves the phenomenon but its design is unlikely to produce data containing any interesting patterns.</td>
<td>The experiment investigates the phenomenon and the data will probably show interesting patterns, but its design will miss some features or patterns.</td>
<td>The experiment investigates the phenomenon; it is highly likely the data will contain interesting patterns with all their features observable.</td>
</tr>
<tr>
<td>3. Decide what to measure; identify the independent and dependent variables.</td>
<td>The chosen measurements will not produce data that can be used to achieve the goals of the experiment.</td>
<td>The chosen measurements will produce only data that is useful (at best) to partially achieve the goals of the experiment.</td>
<td>The chosen measurements will produce data useful in achieving the experiment’s goals, but independent and dependent variables aren’t clearly distinguished.</td>
<td>The chosen measurements will produce data useful for achieving the experiment’s goals. Independent and dependent variables are clearly distinguished.</td>
</tr>
<tr>
<td>4. Use the available equipment to make measurements.</td>
<td>At least one of the chosen measurements cannot be made with the available equipment.</td>
<td>All chosen measurements can be made, but no details are given about how they are done.</td>
<td>All chosen measurements can be made, but the details of how they are done are vague or incomplete.</td>
<td>All chosen measurements can be made and all details of how they are done are clearly provided.</td>
</tr>
<tr>
<td>5. Describe observations without explaining them, using words and a picture of the experimental set-up.</td>
<td>No description is mentioned.</td>
<td>A description is offered but it is incomplete. No picture is present. Or, most of the observations are mentioned in the context of prior knowledge.</td>
<td>The description (with a labeled picture) is given but mixed with explanations/other material. Or, some observations are given in terms of prior knowledge.</td>
<td>Clear descriptions are given of what happens in the experiments—both verbally and via a labeled picture.</td>
</tr>
<tr>
<td>6. Identify the short-comings in the experimental design—and suggest improvements.</td>
<td>No attempt is made to identify any shortcomings of the experimental design.</td>
<td>Some shortcomings are described—but vaguely—with no suggestions for improvements.</td>
<td>Some shortcomings are identified and some improvements are offered, but not all aspects of the design are considered.</td>
<td>All major shortcomings of the experiment are identified and specific suggestions for improvement are made.</td>
</tr>
<tr>
<td>7. Construct a mathematical relationship (if applicable) that represents a trend in the data.</td>
<td>No attempt is made (if applicable) to construct a relationship that represents a trend in the data.</td>
<td>An attempt is made (if applicable), but the relationship suggested does not represent the trend in the data.</td>
<td>The relationship (if applicable) represents the trend, but there is no analysis of how well it fits the data. Or, some features of the relationship are missing.</td>
<td>The relationship (if applicable) represents the trend accurately and completely, and an analysis of how well it agrees with the data is included.</td>
</tr>
<tr>
<td>8. Devise an explanation for an observed relationship.</td>
<td>No attempt is made to explain the observed relationship.</td>
<td>An explanation is offered, but it is vague, or not testable, or it contradicts the observations.</td>
<td>An explanation is made and is based on simplifying the phenomenon, but it uses flawed reasoning.</td>
<td>A reasonable explanation is made and is based on simplifying the phenomenon.</td>
</tr>
<tr>
<td>9. Identify the assumptions made in devising the explanation.</td>
<td>No attempt is made to identify any assumptions.</td>
<td>An attempt is made to identify assumptions, but most are missing, described vaguely, or incorrect.</td>
<td>Most assumptions are correctly identified.</td>
<td>All assumptions are correctly identified.</td>
</tr>
</tbody>
</table>
### Rubric T: Testing experiment

<table>
<thead>
<tr>
<th>Scientific Ability</th>
<th>Missing (0 points)</th>
<th>Inadequate (1 point)</th>
<th>Still needs improvement (2 points)</th>
<th>Adequate (3 points)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Clearly identify the hypothesis to be tested.</td>
<td>No mention is made of a hypothesis to be tested.</td>
<td>An attempt is made to identify the hypothesis to be tested, but it is described in a confusing manner.</td>
<td>The hypothesis to be tested is described, but there are minor omissions or vague details.</td>
<td>The hypothesis is clearly stated.</td>
</tr>
<tr>
<td>2. Design a reliable experiment that tests the hypothesis.</td>
<td>The experiment does not test the hypothesis.</td>
<td>The experiment tests the hypothesis, but due to the nature of the design it is likely the data will lead to an incorrect judgment.</td>
<td>The experiment tests the hypothesis, but due to the nature of the design, there is a moderate chance that the data will lead to an inconclusive judgment.</td>
<td>The experiment tests the hypothesis and has a high likelihood of producing data that will lead to a conclusive judgment.</td>
</tr>
<tr>
<td>3. Distinguish between a hypothesis and a prediction.</td>
<td>No prediction is made. The experiment is not treated as a testing experiment.</td>
<td>A “prediction” is made, but it is identical to the hypothesis.</td>
<td>A prediction is made and is distinct from the hypothesis but does not describe the outcome of the designed experiment.</td>
<td>A prediction is made that is distinct from the hypothesis, and it describes the outcome of the designed experiment.</td>
</tr>
<tr>
<td>4. Make a reasonable prediction based upon a hypothesis.</td>
<td>No prediction is attempted.</td>
<td>A prediction (distinct from the hypothesis) is made, but it is not based on the hypothesis.</td>
<td>A prediction is made that follows from the hypothesis, but it does not incorporate assumptions.</td>
<td>A prediction is made that follows from the hypothesis and incorporates assumptions.</td>
</tr>
<tr>
<td>5. Identify the assumptions made in making the prediction.</td>
<td>No attempt is made to identify any assumptions.</td>
<td>An attempt is made to identify assumptions, but the assumptions are either irrelevant or confused with the hypothesis.</td>
<td>Relevant assumptions are identified but are not significant for making the prediction.</td>
<td>All assumptions are correctly identified.</td>
</tr>
<tr>
<td>6. Identify specifically how the assumptions might affect the prediction.</td>
<td>No attempt is made to determine the effects of assumptions.</td>
<td>The effects of assumptions are mentioned but are described vaguely.</td>
<td>The effects of assumptions are determined, but no attempts are made to validate them.</td>
<td>The effects of the assumptions are determined and the assumptions are validated.</td>
</tr>
<tr>
<td>7. Decide whether the prediction and the outcome agree or disagree.</td>
<td>There is no mention made as to whether the prediction and outcome agree or disagree.</td>
<td>A decision is made about the agreement or disagreement, but it’s not consistent with the outcome of the experiment.</td>
<td>A reasonable decision about the agreement or disagreement is made, but experimental uncertainty is not taken into account.</td>
<td>A reasonable decision about the agreement or disagreement is made, and experimental uncertainty is taken into account.</td>
</tr>
<tr>
<td>8. Make a reasonable judgment about the hypothesis.</td>
<td>No judgment is made about the hypothesis.</td>
<td>A judgment is made but is not consistent with the outcome of the experiment.</td>
<td>A judgment is made and is consistent with the outcome of the experiment, but assumptions are not taken into account.</td>
<td>A reasonable judgment is made and assumptions are taken into account.</td>
</tr>
<tr>
<td>9. Revise the hypothesis if/when necessary.</td>
<td>A revision is necessary but none is made.</td>
<td>A revision is necessary and attempted, but the new hypothesis is not consistent with the results of the experiment.</td>
<td>A revision is necessary, and one is suggested that is consistent with the results of the experiment, but other relevant evidence is not taken into account.</td>
<td>A necessary revision is made and is consistent with all relevant evidence.</td>
</tr>
</tbody>
</table>
### Rubric A: Application experiment

<table>
<thead>
<tr>
<th>Scientific Ability</th>
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<th>Still needs improvement (2 points)</th>
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</tr>
</thead>
<tbody>
<tr>
<td>1. Clearly identify the problem to be solved.</td>
<td>No mention is made of the problem to be solved.</td>
<td>An attempt is made to identify the problem to be solved, but it is described in a confusing manner.</td>
<td>The problem to be solved is described, but there are minor omissions or vague details.</td>
<td>The problem to be solved is clearly stated.</td>
</tr>
<tr>
<td>2. Design a reliable experiment that solves the problem.</td>
<td>The experiment does not solve the problem.</td>
<td>The experiment attempts to solve the problem but due to the nature of the design the data will not lead to a reliable solution.</td>
<td>The experiment attempts to solve the problem but its design allows a moderate chance that the data will not lead to a reliable solution.</td>
<td>The experiment solves the problem and has a high likelihood of producing data that will lead to a reliable solution.</td>
</tr>
<tr>
<td>3. Use available equipment to make measurements.</td>
<td>At least one of the chosen measurements cannot be made with the available equipment.</td>
<td>All of the chosen measurements can be made, but no details are given about how it is done.</td>
<td>All of the chosen measurements can be made, but the details about how they are done are either vague or incomplete.</td>
<td>All of the chosen measurements can be made, and all details about how they are done are clearly provided.</td>
</tr>
<tr>
<td>4. Make a judgment about the results of the experiment.</td>
<td>No discussion is presented about the results of the experiment.</td>
<td>A judgment is made about the results, but it is not reasonable or coherent.</td>
<td>An acceptable judgment is made about the result, but the reasoning is flawed or incomplete.</td>
<td>An acceptable judgment is made about the result, with clear reasoning. The effects of assumptions and experimental uncertainties are considered.</td>
</tr>
<tr>
<td>5. Evaluate the results using an independent method.</td>
<td>No attempt is made to evaluate the consistency of the result using an independent method.</td>
<td>An independent method is used to evaluate the results. However there is little or no discussion about the differences in the results of the two methods.</td>
<td>An independent method is used to evaluate results, with some discussion of the differences in results, but little about possible reasons for the differences.</td>
<td>An independent method is used to evaluate the results. Discrepancies between the methods’ results—reasons, % difference (if applicable) — are discussed.</td>
</tr>
<tr>
<td>6. Identify the shortcomings in an experimental design and suggest specific improvements.</td>
<td>No attempt is made to identify any shortcomings of the experimental design.</td>
<td>An attempt is made to identify shortcomings, but they are described vaguely and without specific suggestions for improvements.</td>
<td>Some shortcomings are identified, and some improvements are suggested, but not all aspects of the design are considered.</td>
<td>All major shortcomings of the experiment are identified and specific suggestions for improvement are made.</td>
</tr>
<tr>
<td>7. Choose a useful mathematical procedure for solving the experimental problem.</td>
<td>Either there is simply no mathematical procedure included, or the procedure included is irrelevant to the design.</td>
<td>A mathematical procedure is described, but it is incomplete, and therefore the final answer cannot be calculated.</td>
<td>A correct and complete mathematical procedure is described, but an error is made in the calculations.</td>
<td>A complete mathematical procedure described, fully consistent with the design. All quantities are calculated correctly, and the final answer is meaningful.</td>
</tr>
<tr>
<td>8. Identify the assumptions made in using the mathematical procedure</td>
<td>No attempt is made to identify any assumptions.</td>
<td>An attempt is made to identify assumptions, but most are missing, described vaguely, or incorrect.</td>
<td>Most assumptions are correctly identified.</td>
<td>All assumptions are correctly identified.</td>
</tr>
<tr>
<td>9. Determine specifically the way(s) in which assumptions might affect the results.</td>
<td>No attempt is made to determine the effects of assumptions.</td>
<td>An attempt is made to determine the effects of some assumptions, but most are missing, described vaguely, or incorrect.</td>
<td>The effects of most (but not all) assumptions are determined correctly, and/or a few contain errors or inconsistencies.</td>
<td>The effects of all assumptions are correctly determined.</td>
</tr>
</tbody>
</table>
Experimental Uncertainty

You can’t measure any physical quantity exactly. You can say only that its value lies within a certain range of uncertainty. Therefore, as an experimenter measuring any value, X, you must make a judgment that the “true” value of X lies somewhere between X – ΔX and X + ΔX (usually expressed in the standard form, X ± ΔX).

Why is this important? Why do you need to know about uncertainty—and how to estimate it? Because otherwise you can’t answer even the simplest questions in scientific experimentation. For example:

“Is the measured value in agreement with the prediction?”

“Do the data fit the physical model?”

To answer either of these questions, you need to use numbers— the data you’ve measured. But what value(s) should you use, when all of them contain uncertainties?

Consider even the most basic physical question:

“Are two measured values, X and Y, different or the same?”

Your measurements may show them to be slightly different, but what if that difference is smaller than the uncertainty with which you can measure them? If the ranges X ± ΔX and Y ± ΔY overlap, then you cannot make a valid argument that X and Y are actually different. You must declare that they are the same within your experimental uncertainty.

The issue of uncertainty directly impacts your physics lab measurements and conclusions. You’ll need to be aware of it not only as you make your experimental measurements, but much earlier, too—as you design those experiments in the first place.

All in all, to correctly and completely analyze your experimental results, you’ll need to know...

• How to identify the sources of measurement uncertainty.
• How to estimate the quantitative effects (magnitude and sign) of each source of uncertainty.
• How to compare seemingly unlike types and magnitudes of uncertainties—by converting them to relative uncertainties.
• How to make measurements in ways that reduce their relative uncertainties.
• How to account for various combinations of (relative) uncertainties as you calculate results using more than one measured value: Are the uncertainties about equal, or is one significantly larger than the rest?

Here’s a short look at each of the above....
Sources of Uncertainty in Measurements

**Instrumental uncertainties.** Every measuring instrument has an inherent uncertainty that is determined by the precision of that instrument.

How can you estimate (quantify) instrumental uncertainty? Usually its absolute value is half of the smallest increment of the instrument scale. For example, if the most finely spaced marks on a ruler are 1 millimeter apart, then 0.5 mm is that ruler’s precision. Likewise, a clock marked with 1-second intervals has a precision of 0.5 s.

Instrumental sources of uncertainty are the easiest to estimate, but unfortunately they’re not the only sources—and often not even the most significant. You’d have to be a very skillful (and lucky) experimentalist indeed to eliminate all other sources of uncertainty; the overall uncertainty of the measurement is almost never equal to the instrumental uncertainty.

**Random uncertainties.** Often when you measure the same quantity more than once, you’ll get a slightly different value each time—due to various uncontrollable factors that can randomly affect your results.

How can you estimate (quantify) random uncertainty? You must repeat the measurement several times, take an average, then look at how far the data typically vary from that average.

For example, if you are measuring the distance at which a cannonball hits the ground, you could get a slightly different distance every time you repeat the shot—say 50 m, 51 m and 49 m. The average is then \((50+51+49)/3 = 50\) m. And the data values are spread around this average by about a meter: \(X = 50\) m ± 1 m. Or, in other words: \(|\Delta X| = 1\) m.

You’d therefore estimate that (speaking for the moment only of random uncertainty) most cannonballs will fall in the range from 49 m to 51 m (i.e. from \(X - \Delta X\) to \(X + \Delta X\)).

**Uncertainties due to experimental design and assumptions.** The simplifying assumptions that are inherent in your model may also contribute to the uncertainty of the desired quantity. For example, suppose you’re measuring the diameter of a baseball and are assuming it is perfect sphere. But its actual diameter may differ by about a millimeter, depending what axis you measure across (and the seams are yet another question).

This type of uncertainty is not easy to recognize, let alone evaluate. First of all, you have to determine the nature of the effect (whether the assumption increases or decreases the measured value—or affects it randomly). Then you must somehow estimate the magnitude of the effect. As another example, suppose you wish to find the speed of a ball moving on the floor. You are assuming that a ball moves along a straight line while in fact the surface of the floor is bumpy—and the bumps contribute significantly to the distance that the ball covers, thus decreasing the speed that that you calculate. Note that, while there is a certain randomness in the amount of “bumpiness” encountered by the ball in each particular trial, the effect is always to decrease your result—it’s not truly random; and repeating the measurement will not eliminate this effect.

As you can see, it is difficult to give strict rules and instructions on how to estimate uncertainties in general. Each case (each measurement within each experimental design) is unique and requires a thoughtful approach.

The best advice: Be observant—and then reasonable.
Comparing Uncertainties

If you’re comparing the uncertainties in the values of two different quantities, then analyzing the absolute uncertainty ranges won’t tell you which of the measurements is more accurate. Even if you’re making the same type of measurement (say, cm), the absolute amount of the uncertainty can have a larger or smaller effect, depending on the value of the measurement itself. (And then what if the units or dimensions of the two quantities are different?) How can we decide which quantity has a larger uncertainty?

In general, we need to compare relative uncertainties—taking, for each measurement, the ratio of the absolute uncertainty to the quantity itself: \( \Delta X / X \). You can express this as a fraction (decimal) or as a percentage (by multiplying by 100%).

Even our very senses operate on relative uncertainty. The thickness of the “fuzzy” edge is the same (9 units) for both blue circles, but the larger blue circle (90 units) looks sharper than the small one (30 units). That happens because we unconsciously compare relative uncertainties (which are 10% for the large circle; 30% for the small one).

Note here: Some measurements, such as temperature, are not absolute in the first place; it is actually the change in the measured value(s) that you’re interested in. Consider a thermometer known to be reliable to \( \pm 0.5^\circ\text{C} \). Does this mean you have a 0.5% uncertainty in measuring the temperature of 100°C water—but a 10% uncertainty when using the same thermometer in cold water at 5°C? (No.) But even if you express the temperatures on an absolute scale (Kelvins), that’s still not an accurate accounting for the relative uncertainty of your measurements. After all, a single temperature reading is unlikely to be experimentally significant; usually you’re measuring a change—a difference. And so you’d compare the uncertainty of the difference to the calculated difference itself. (see the next page for more about calculating with uncertainties).

Reducing Uncertainties

The above example with the circles suggests one way to reduce the relative uncertainty in your measurement: The same absolute uncertainty will yield a smaller relative uncertainty if the measured value is larger.

Example: Suppose you want to measure the time interval needed for a bob on a spring to oscillate up and down once. If you’re using a watch to measure that interval, the absolute uncertainty of the measurement will be 0.5 s. And if you measure, say, 5 s as the interval, then your relative uncertainty will be \( (0.5 \text{ s}/5 \text{ s}) \cdot 100\% = \pm 10\% \).

But suppose you instead measure the time interval for 5 oscillations (25 s). It’s still a single measurement, so the instrumental uncertainty is still 0.5 s, but now the relative uncertainty is \( (0.5 \text{ s}/25 \text{ s}) \cdot 100\% = \pm 2\% \).

It’s a simple technique, but effective. Just don’t rely on it alone. Don’t overlook ways to reduce your relative uncertainties by minimizing the absolute uncertainties, whenever possible (e.g. by using better design, or fewer assumptions, or measuring instruments of greater precision).
Calculating with Measured Values: Combining Uncertainties

Uncertainties in your data measurements will propagate through any calculations you make with those data, producing uncertainties in the calculated results. For example, suppose you know the average mass, \( m \), of one apple, with an uncertainty \( \Delta m \). If you want then to calculate the mass, \( M \), of a basket of, say, 100 apples, you will get \( M \pm \Delta M = 100m \pm 100\Delta m \). Thus, in this case, the relative uncertainty of the calculated value \( M \) remains the same as the relative uncertainty of the single measurement: \( \Delta M / M = \Delta m / m \). However, if you are using more than one measured value in your calculation, estimating the uncertainty of the calculated result is more complicated.

**Comparable uncertainties**: If your measured values have comparable relative uncertainties, then the uncertainty in a calculation using those values depends on the specific math you use in the calculation. There are many cases, therefore—and entire books on the topic—but take some common examples here:

- When you **add or subtract** two measured values, their **absolute** uncertainties **add**. By extension, therefore, taking a multiple of a single measured value (which is, essentially, “adding it to itself”) simply multiplies the absolute uncertainty—see the basket of apples above. A **coefficient multiplies the absolute uncertainty**.

- When you **multiply or divide** two measured values, their **relative** uncertainties **add**. By extension, therefore, squaring a measured value (raising it to the 2nd power) will double the relative uncertainty; and cubing a measured value (raising it to the 3rd power) will triple the relative uncertainty; etc. (Thus, in the baseball example earlier, if you use your diameter measurement to calculate the volume of the ball—assuming it to be spherical—the relative uncertainty in the calculated volume will be three times larger than the relative uncertainty in the measured diameter.) An **exponent multiplies the relative uncertainty**.

**Unequal uncertainties (the “weakest link” rule)**: The relative uncertainty in any calculated value is always at least as great as the greatest relative uncertainty among the values used to make the calculation. Therefore, if one of your measurements has a relative uncertainty much larger than any of the others, then that measurement is your “weakest link”—you can generally ignore the other, insignificant uncertainties and take the uncertainty of the calculation to be that of the most uncertain measurement.

**Your Lab Strategy for Uncertainty: A Summary**

When you are designing a lab experiment and measuring some quantities to determine an experimental result:

- Decide which factors affect your result most; wherever possible, try to minimize these factors.
- Wherever possible, try to reduce unavoidable uncertainties by measuring longer distances or times etc.
- Decide what the absolute uncertainties of each measurement are.
- Then find the relative uncertainties of each measurement.
- If you need to do any **calculations** with your measurements, then:
  - If the measurements have relative uncertainties of comparable magnitude, use the math rules above (and if you need more rules, find an online resource); but if one relative uncertainty is much larger than all the others, ignore the others and use the largest as the uncertainty of the calculated result.
- **Find the range where your experimental result lies; and take into account its uncertainty when you make a judgment regarding that result and the experiment’s outcome**.
LAB 1: Introduction and Math Review

I. Introduction to Lab/Course Policies

II. Vector Math Review.

Because you will not be going to lab in Week 1, this is a good time to learn lab and course policies and refresh some vector math basics. So, unlike the other labs this term, this first lab activity is not the usual 3-hour, in-lab group-work format. Rather, it’s a take-home assignment that each student must do (worth 10 points)—to be turned in to your Lab TA’s box by 6:00 p.m. on Tuesday, April 10.

Click here to download these activities (it’s just one combined file for both parts I and II).